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Aperture Determination by Long Term and Multiparticle Tracking

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RHIC PROJECT

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APERTURE DETERMINATION BY LONG TERM & MULTIPARTICLE TRACKING*

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Abstract

Apertures determined by long term tracking for 10^6 turns at $\beta^* = 2$m and 6m and tracking of 100 particles for 1000 turns at $\beta^* = 2$m are reported. The multiparticle results are consistent with the aperture determined from 10^6 turn runs. Finally, the 10^6 turn results are extrapolated to 3×10^9 turns to obtain an estimate of the aperture for which particles survive for 10 hours in RHIC.

I. INTRODUCTION

Studies of long term stability in RHIC are reported. The results were obtained from two independent studies using different tracking programs on different computers. Only transverse motion was considered; the effects produced by synchrotron oscillation and tune ripple were not included.

The relation $B = B_o \sum (bn + i\, an)(X + i\, Y)^n$ was used for the field expansion. Multipoles coefficients a_n and b_n were generated according to a Gaussian distribution that was truncated at $\pm 3\sigma$. Apertures, based on the worst of ten cases, are quoted in terms of the initial amplitude X_i in a focusing quadrupole having $\beta_x = 50$m when the initial emittances in the X and Y planes are equal.

II. APERTURE DETERMINATION

A. ORBIT

Studies with the ORBIT tracking program were made at $\beta^* = 2$m and $\beta^* = 6$m in all six insertions. Ten distributions of random field errors were used with multipoles of order $2 \leq n \leq 10$ included. Stability at 10^6 turns was determined when an amplitude test of 60mm was used as a measure of the dynamic aperture. Runs with one seed were continued until the motion became unstable at 8.8×10^6 turns. The aperture determined by a survival plot is extrapolated to 3×10^9 turns that corresponds to a lifetime of 10 hours in RHIC. The dynamic aperture at $\beta^* = 2$m decreases 20% when runs are extended from 400 to 10^6 turns. A simple extrapolation to 3×10^9 turns, which may be pessimistic, produces an additional 20% aperture decrease. The results are shown in Figure 1.

Similar runs made with $\beta^* = 6$m show little change in the dynamic aperture as runs are extended from 400 to 10^6 turns. Survival plots for $\beta^* = 6$m are shown in Figure 2.

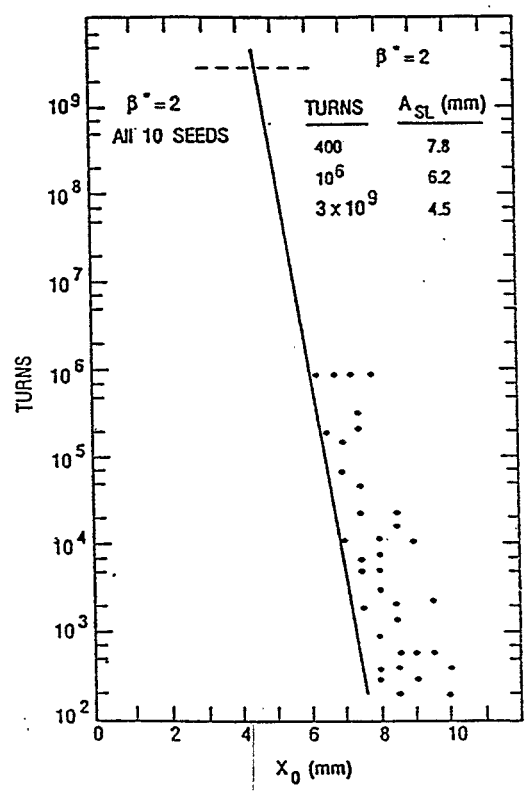

Figure 1: Survival times versus particle amplitude X_o. $\beta^* = 2$ m. Ten distributions of random field errors.

B. PATRICIA

Aperture studies were made with the PATRICIA program with $\beta^* = 2$m in all insertions and the tune was $\nu_x = 28.826$ and $\nu_y = 28.820$. Multipole expansions for fields were made for $2 \leq n \leq 16$ in dipoles and $2 \leq n \leq 10$ in quadrupoles; multipoles were present in all elements of the arcs and insertions. The amplitude was tested at every element to assure the particle remains within the vacuum chamber.

B.1. Long Term Tracking

Stability at 10^6 turns was determined for ten distributions of random field errors when test particles were launched with $\epsilon_x = \epsilon_y$ and $X' = Y' = 0$. Histories for the worst cases, seeds #9 and #10, and the best case, seed

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#1, are shown in Figure 3. Points at values $< 10^6$ indicate failure; points at 10^6 turns indicate survival. Some seeds indicate sharp reductions in survival as the initial amplitude is decreased. For seed # 9 the particle survived for 84K turns at $X_i = 7.3$mm but failed after 6,130 turns at an amplitude of 6.7mm. For 10^6 turn runs, the acceptance of RHIC is 6.2mm as compared with 7.6mm for 1000 turn runs.

B.2. Multiparticle Tracking

Determination of ϵ_x and ϵ_y after each turn indicates there is transfer of emittance between the X and Y planes and that the total emittance is not always conserved. This is shown in Figure 4. The emittance transfer is repetitive with a period of $\cong 150$ turns but does not include points having $\epsilon_x/\epsilon_t(o) \cong 1$. Runs were made to determine whether the aperture is independent of the initial coordinates (X, X', Y, Y') of the particles. We select ϵ_x randomly in the range $0 < \epsilon_x < \epsilon_t(o)$, use $\epsilon_y = \epsilon_t(o) - \epsilon_x$, and determine X, X', consistent with ϵ_x, and Y, Y', consistent with ϵ_y.

At each amplitude, 100 particles were tracked for 1000 turns. Tracking was performed at the total emittance $\epsilon_t(o)$ for which particles, launched with $\epsilon_x = \epsilon_y$ and $X' = Y' = 0$, survived 10^6 turns. Of the ten cases studied, five were stable, two showed 2.5% aperture decrease, and three showed aperture decreases between 8 and 14%. For RN#1, the machine showing the largest aperture for the 10^6 turn runs, 35 of the 100 particles failed within 1000 turns.

The sequence of random numbers used for multiparticle launching differs for different seeds, and hence particles are launched with different X, X', Y and Y'. This possible source of difference was checked by resetting the random number generator of all machines to the value used for the machine having the smallest aperture. This gives the same relative X, X', Y and Y' for each machine. The five machines showing stability again had no failures when 100 particles were tracked for 1000 turns.

A test was also made to determine if the aperture for these five machines is larger than that obtained from long term tracking. This was confirmed; a comparison of results from 10^6 turn runs and multiparticle runs are shown in Figure 5.

III. DISCUSSION

For the 10^6 runs, particles were launched with $\epsilon_x = \epsilon_y = \epsilon_t/2$. These runs most often showed more complete emittance transfer to the Y plane than to the X plane. For multiparticle tracking, no limitation was placed on the initial ratio of ϵ_x/ϵ_t. Some failures result from particles with ϵ_x/ϵ_t outside the range observed during the 1×10^6 turn studies. Four out of five seeds showing decreased

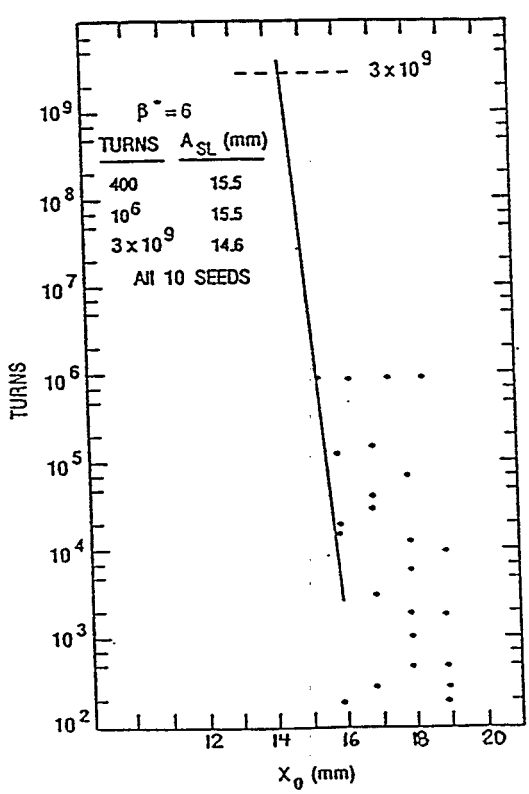

Figure 2: Survival times versus particle amplitude X_o. $\beta^* = 6$ m. Ten distributions of random field errors.

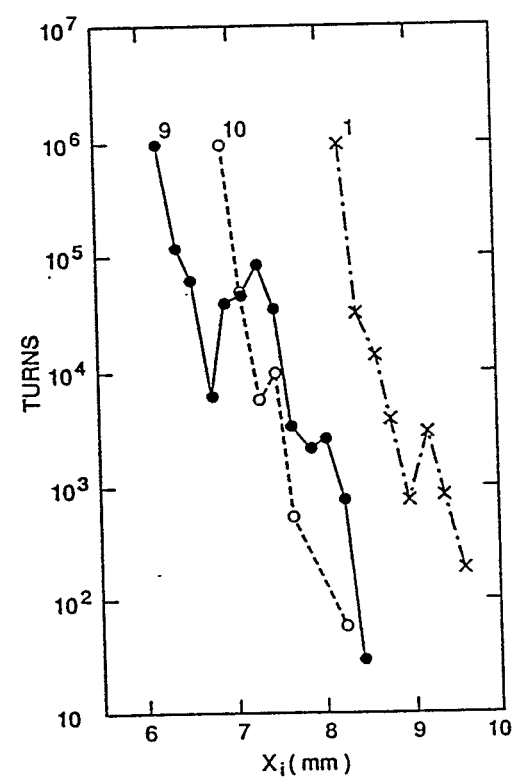

Figure 3: Dependence of particle survival on initial amplitude for three distributions of random field errors: worst cases (9&10), and best case (1).

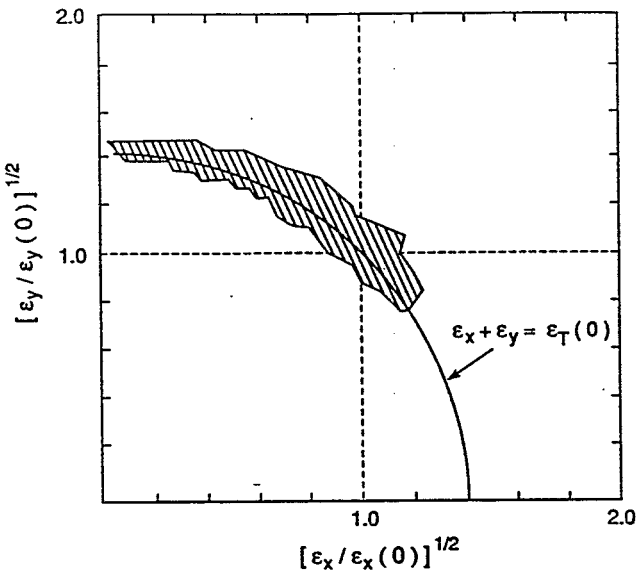

Figure 4: Dependence of $\sqrt{\epsilon_y}$ on $\sqrt{\epsilon_x}$ during a 500 turn run. Seed #5.

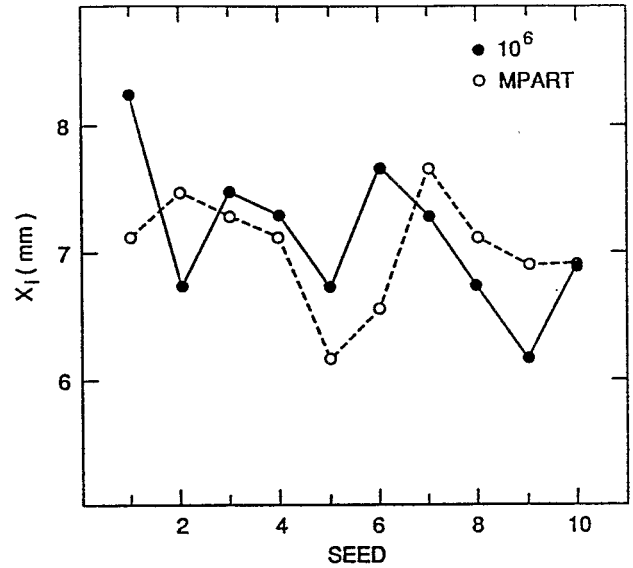

Figure 5: Comparison of aperture determinations from long term (10^6) and multiparticle (MP) tracking runs for ten distributions of random field errors.

Table 1: Summary of Aperture Determinations.

	β^*(m)	TURNS 400 (mm)	10^6 (mm)	1000(MP) (mm)
ORBIT	2	7.8	6.2	
PATRICIA	2	7.6	6.2	6.2
ORBIT	6	15.5	15.5	

aperture for the multiparticle runs were launched with $\epsilon_t/\epsilon_t \geq 0.84$ (a region infrequently encountered in the 10^6 turn runs), and four of five seeds showing increased aperture had $\epsilon_x/\epsilon_t \leq 0.53$ a region frequently encountered in the 10^6 turn runs.

We conclude that multiparticle tracking using many sets of launching coordinates can provide a test of particle stability in regions where launching with $\epsilon_x = \epsilon_y$ and $X' = Y' = 0$ seems stable. An example is provided by machine #5 for which failure at $X = 6.9$mm was experienced after 573K turns, while 17 of 100 particles having the same emittance failed within 1000 turns when launched in the multiparticle mode. Multiparticle tracking complements long term tracking by probing areas of (X, X', Y, Y') space not available to particles launched with $\epsilon_x = \epsilon_y$ and $X' = Y' = 0$. The results are summarized in Table 1.

IV. ACKNOWLEDGMENTS

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V. REFERENCES

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[2] V. Visnjic, Fermilab Publication 90/80 (1990).